

Syllabus for Math 416 (M13)

Instructor: S. P. Dutta, TR 11:00-12:20pm

Course summary: Math 416 is a rigorous, abstract treatment of linear algebra. Topics to be covered include vector spaces, linear transformations, eigenvalues and eigenvectors, diagonalizability, and inner product spaces. The course concludes with a brief introduction to the theory of canonical forms for matrices and linear transformations.

Book: The textbook for the course is Linear Algebra, fourth edition, by S. H. Friedberg, A. J. Insel and L. E. Spence

Syllabus: The essential ideas in the course are

- (1) systems of linear equations, row reduction and echelon form
- (2) vectors and matrices, matrix multiplication, invertibility and inverses
- (3) vector spaces and linear transformations
- (4) subspaces, linear combinations, spanning sets and bases
- (5) representing linear transformations as matrices, change of basis
- (6) kernel and image, row and column rank, Rank-Nullity theorem
- (7) determinants
- (8) eigenvalues and eigenvectors
- (9) finding the eigenvalues of a transformation using the characteristic polynomial
- (10) finding the eigenspace associated to an eigenvalue
- (11) inner product spaces and their algebra and geometry, the Cauchy–Schwarz inequality
- (12) orthogonal projections, Gram–Schmidt, least squares
- (13) orthogonal and unitary matrices, spectral theory
- (14) bilinear forms
- (15) Jordan form