# Charles W. Rezk

Curriculum Vitae

	Department of Mathematics University of Illinois 1409 W. Green St. Urbana, IL 61801	phone: (217) 265-6309 fax: (217) 333-9576 email: rezk@illinois.edu
Education	<b>University of Pennsylvania</b> (Philadelphia, PA) B.A. in mathematics, May 1991. M.A. in mathematics, May 1991.	1987—1991
	Massachusetts Institute of Technology (Cambridge, MA) Ph.D. in pure mathematics. Date of graduation: May 1996. Thesis title: "Spaces of Algebra Structures and Cohomology of Og Thesis advisor: Michael J. Hopkins.	<i>1991—1996</i> perads."
Academic Positions	Northwestern University (Evanston, IL) Ralph P. Boas Visiting Assistant Professor (9/1996–8/1999). Instructor (9/1999–8/2001).	1996—2001
	<b>University of Illinois at Urbana-Champaign</b> (Urbana, IL) Assistant Professor of Mathematics Associate Professor of Mathematics Professor of Mathematics	2001—2006 2006—2014 2014—present
Visiting Positions	Institute for Advanced Study, (Princeton, NJ) $9/1999-3/2000$ and $1/2001-3/2001$ Member	
	<b>Massachusetts Institute of Technology</b> (Cambridge, MA) Visiting instructor	1/2006-5/2006
	Mathematical Sciences Research Institute (Berkeley, CA) Simons Visiting Professor	1/2014-5/2014
Honors	Alfred P. Sloan Doctoral Dissertation Fellowship AMS Centennial Fellowship Fellow of the AMS	1995—1996 1999—2000 2014
Service	Editorial board, Compositio Mathematica	2015-2021

## Charles W. Rezk

Publications and Creative Works<sup>1</sup>

**Doctoral Thesis.** "Spaces of Algebra Structures and Cohomology of Operads." (MIT, 1996)

### Publications.

- "Notes on the Hopkins-Miller theorem." In Homotopy Theory via Algebraic Geometry and Group Representations, Contemporary Mathematics 220, Amer. Math. Soc., 1998, pp. 313-366.
- "Brown-Comenetz duality and the Adams spectral sequence," with Mark Mahowald. In American Journal of Mathematics 121 (1999), pp. 1153–1177.
- 3. "A model for the homotopy theory of homotopy theory." Trans. Am. Math. Soc. **353** (2001), 973–1007.
- 4. "Simplicial structures on model categories and functors," with B. Shipley and S. Schwede. Am. J. of Math. **123** (2001), 551–575.
- 5. "Every homotopy theory of simplicial algebras admits a proper model." *Topology* and its Applications, **119** (2002), 65–94.
- 6. "A resolution of the K(2)-local sphere at the prime 3," with P. Goerss, H.-W. Henn, and M. Mahowald. Annals of Mathematics, **162** (2005), 777–822.
- 7. "The units of a ring spectrum and a logarithmic cohomology operation." Journal of the American Mathematical Society, **19** (2006), 969–1014.
- "Topological modular forms of level 3," with M. Mahowald. Pure and Applied Math. Quarterly, 5 (2009), 853–872.
- "A cartesian presentation of weak n-categories." Geometry & Topology, 14 (2010), 521–571. "Correction to 'A cartesian presentation of weak n-categories'." Geometry & Topology, 14 (2010), 2301–2304.
- 10. "The congruence condition for power operations in Morava *E*-theory." *Homology*, *Homotopy*, and *Applications*, **11** (2010), 327–379.
- "Modular isogeny complexes." Algebraic & Geometric Topology, 12 (2012), 1373– 1404.
- "Reedy categories and the Θ-construction," with J. Bergner. Mathematische Zeitschrift, 274 (2013), 499-514.
- 13. "A streamlined proof of Goodwillie's *n*-excisive approximation." Algebraic & Geometric Topology, **13** (2013), 1049–1051.
- 14. "Comparison of models for  $(\infty, n)$ -categories, I," with J. Bergner. Geometry & Topology, **17** (2013), 2163–2202.

<sup>&</sup>lt;sup>1</sup>All papers and preprints are available from https://faculty.math.illinois.edu/~rezk.

- "An ∞-categorical approach to *R*-line bundles, *R*-module Thom spectra, and twisted *R*-homology," with M. Ando, A. Blumberg, D. Gepner, and M. Hopkins. Journal of Topology 7 (2014), 869–893.
- "Units of ring spectra and Thom spectra via structured ring spectra," with M. Ando, A. Blumberg, D. Gepner, and M. Hopkins. *Journal of Topology* 7 (2014), 1077–1117.
- 17. "On Hopkins' Picard groups for the prime 3 and chromatic level 2", with P. Goerss, H.-W. Henn, and M. Mahowald. *Journal of Topology* 8 (2015), 267–294.
- 18. "Isogenies, power operations, and homotopy theory." In *Proceedings of the ICM*, Seoul 2014, vol. 2 (2014), 1125–1146.
- 19. "Spectral algebra models of unstable  $v_n$ -periodic homotopy theory." To appear in Surveys around Ohkawa's theorem on Bousfield classes. (arXiv:1703.02186)
- 20. "Classifying spaces for 1-truncated compact Lie groups." Algebraic & Geometric Topology 18 (2018), 525–546.
- 21. "Spectral algebra models of unstable  $v_n$ -periodic homotopy theory," with M. Behrens. 45 pages. In *Bousfield classes and Ohkawa's theorem*, Springer Proc. Math. Stat., 309, Singapore, 2020.
- 22. "Looijenga line bundles in complex analytic elliptic cohomology." Tunisian Journal of Mathematics 2 (2019), 1–42.
- "The Bousfield-Kuhn functor and topological André-Quillen cohomology", with M. Behrens, *Inventiones Mathematicae*, **220** (2020), 949-1022.
- 24. "Comparison of models of  $(\infty, n)$ -categories, II", Journal of Topology, **13** (2020), 1554-1581.
- 25. "Spectral algebra models of unstable  $v_n$ -periodic homotopy theory," 45 pages. In Surveys around Ohkawa's theorem on Bousfield classes, Springer Proceedings in Mathematics and Statistics 309, Springer, 2020, 275-323.
- 26. "Spectral algebraic geometry." To appear as a chapter in *Stable categories and structured ring spectra*, edited by A. Blumberg, T. Gerhardt, M. Hill. MSRI Publications.

#### Conference proceedings edited.

 Homotopy theory: Tools and applications, with Daniel G. Davis, Hans-Werner Henn, J.F. Jardine, Mark W. Johnson, eds. Contemporary Mathematics 729, AMS, 2019.

#### Works submitted for publication and other preprints.

- 1. "Rings of power operations for Morava *E*-theories are Koszul." (arXiv:1204.4831)
- 2. "Free colimit completions of  $\infty$ -categories." (arXiv:2210.08582)

#### Selected invited presentations at conferences.

- May 15, 2007 Workshop on Stacks in Geometry and Topology, Fields Instutute, Toronto – "Morava E-theory of commutative S-algebras and the Frobenius congruence"
- Aug 9, 2007 Abel Symposium, Oslo, Norway "Colinear approximations to homotopy theory"
- Jun 26, 2008 Homotopical Group Theory and Topological Algebraic Topology (invited), Bonn, Germany – "The Frobenius congruence for power operations in Morava E-theory"
- Jun 30, 2008 HOCAT 2008: Homotopy Structures in Geometry and Algebra (invited), CRM, Barcelona, Spain – "Homotopy theory and (∞, 1)-categories"
- May 28, 2009 Topological Field Theories Conference, Northwestern "Cartesian presentations of weak n-categories"
- June 11, 2012 Virginia Topology conference, U. of Virginia "Power operations in ellitpic cohomology"
- March 27, 2013 Equivariant, Chromatic, and Motivic Homotopy Theory, Northwestern University "Power operations at height 2"
- May 11, 2013 Midwest Topology Seminar, U. of Kentucky, Lexington "*p*-isogeny modules, and calculations in multiplicative stable homotopy at height 2"
- April 10, 2014 Reimagining the Foundations of Algebraic Topology, MSRI "Calculations in multiplicative stable homotopy theory at height 2"
- June 24, 2014 Manifolds, K-theory, and Related Topics, Dubrovnik, Croatia "Koszul resolutions of power operation algebras"
- August 18, 2014 ICM Invited Lecture, Topology Section, Seoul, South Korea "Isogenies, power operations, and homotopy theory"
- June 1-19, 2015 Felix Klein lectures, Hausdorff Institue/Max Planck Institute, Bonn (six 120 minute lectures)
- June 29, 2015 Advances in Homotopy Theory Conference, Strasbourg, France
  "Calculating with power operations for Morava E-theory at height 2"
- October 29, 2016 AMS Sectional Meeting invited address, Minneapolis, MN "On some approximations to homotopy theory"
- June 8, 2017 The Transatlantic Homotopy Theory Conference, Regensburg "Looijenga line bundles and complex analytic elliptic cohomology"
- April 3, 2019 Oberwolfach Arbeitsgemeinschaft: Elliptic cohomology according to Lurie "The eye of the storm: Lubin-Tate spectra"
- June 24-28, 2019 Summer School on Higher Topos Theory and Univalent Foundations "Higher topos theory" (five 90 minute lectures)
- October 5, 2019 Midwest Topology Seminar, U. of Chicago "On maps of  $E_\infty$  and  $H_\infty\text{-ring spectra"}$
- June 25-26, 2021 Toposes Online (IHES) "Higher Topos Theory" (four 60 minute lectures) [zoom]

- February 3, 2022 Princeton algebraic topology seminar "Understanding accessible ∞-categories" [zoom]
- March 20, 2023 Homotopy theory in honor of Paul Goerss, Northwestern "Reflections on free colimit completions"

## Graduate students supervised.

- Rekha Santhanam (Ph.D. student, 2003–May, 2008). Ph.D. Thesis "Units of Equivariant Ring Spectra". Was postdoc at JHU. Currently Asst Prof at IIT Bombay.
- Barry Walker (Ph.D. student, 2004–May, 2008). Ph.D. Thesis "Multiplicative Orientations of K-Theory and *p*-adic analysis". Was instructor at Northwestern. position; has worked recently as a NetMath mentor.
- Nathaniel Stapleton (Ph.D. student, 2006–May, 2011). Ph.D. Thesis "Transchromatic Generalized Character Maps". Was postdoc at MIT, then at MPIM Bonn, then at Regensburg. Currently Asst Prof at U Kentucky, Lexington.
- Peter Nelson (Ph.D. student, 2010–2016). Ph.D. Thesis "A small presentation for Morava *E*-theory power operations". Was a postdoc at University of Haifa.
- Zhen Huan (Ph.D. student, 2010–2017). Ph.D. Thesis "Quasi-elliptic cohomology". Currently a research associate at Sun Yat-sen University, Guangzhuo, China.
- Mychael Sanchez [Smith] (Ph.D. student, 2011–2018). Ph.D. Thesis "Equivariant  $E_{\infty}$ -algebras". Currently an Asst Prof at University of New Mexico, Valencia Campus.
- Nima Rasekh (Ph.D. student, 2013–2018). Ph.D. Thesis "A Theory of Elementary Higher Toposes". Postdoc at EPFL, Lausanne, Switzerland.
- William Balderrama (Ph.D. student, 2016–2021). Ph.D. Thesis "Deformations of Homotopy Theories via Algebraic Theories". Currently a postdoc at U. of Virginia.
- Robert Joseph Rennie (passed prelim Spring 2019, 2017–2022). Currently an instructor at Colorado College.
- Abhra Abir Kundu (passed prelim Fall 2020, 2018–present).
- Heyi Zhu (passed prelim Summer 2021, 2018–present).